Chapter 12 Stable Models/Answer Set Programming

- ASP developed in the late 1990s.
- Introduction to ASP: http://www.kr.tuwien.ac.at/staff/tkren/pub/2009/rw2009-asp.pdf [EIK09] Answer Set Programming: A Primer. T. Eiter, G. Ianni, T. Krennwallner
- XSB: XASP package: embeds stable models into XSB PROLOG programming. Not suitable for this lecture.
- smodels+lparse: http://www.tcs.hut.fi/Software/smodels/

668

SITUATION

Usually a program has several stable models (otherwise, the well-founded model is sufficient!)

- either one total well-founded model or one partial well-founded model,
- and either zero or more total stable models, or zero or more partial stable models
- if the well-founded model is total, then "everything is clear" and it is the only stable model.
- if the well-founded model W(P) = (T, F) is partial, its T and F are "guaranteed". Stable models deal with the atoms that are undefined in the well-founded model (= the intersection of all stable models).

According to Lemma 11.2, each stable model is an extension of $W_P = (T, F)$, i.e., for every 3-stable model (T', F'), $T' \supseteq T$ and $F' \supseteq F$.

Example: Win-Move Game

Consider again the small win-move game from Slides 646 and 654:

```
pos(a). pos(b). pos(c). pos(d).
move(a,b). move(b,a). move(b,c). move(c,d).
win(X) :- move(X,Y), not win(Y).
lose(X) :- pos(X), not win(X).
```

[Filename: Datalog/winmove-small.s]

The well-founded model has been derived on Slide 654:

 $W(P) = (\{win(c), lose(d)\}, \{lose(c), win(d)\})$ is partial, since win(a)/lose(a) and win(b)/lose(b) are undefined.

(Total) Stable Models:

 $\mathcal{S}_1(P) = (\{\text{win}(a), \text{win}(c), \text{lose}(b), \text{lose}(d)\}, \{\text{win}(b), \text{win}(d), \text{lose}(a), \text{lose}(c)\}) \text{ and } \mathcal{S}_1(P) = (\{\text{win}(b), \text{win}(c), \text{lose}(a), \text{lose}(d)\}, \{\text{win}(a), \text{win}(d), \text{lose}(b), \text{lose}(c)\}).$

Here, $W(P) = (\{win(c)\}, \{win(d)\})$ provides the "intended" application-specific interpretation of the result: *c* is won, *d* is lost, *a* and *b* are drawn.

From the stable models one can only conclude that it is possible to "fix" a to be won, and then b would also be lost (or vice versa).

670

Example: Choice between Alternatives

Consider again the program P = "porq" from Slide 634 and 659:

q(a) :- not p(a).

p(a) :- not q(a).

[Filename: Datalog/porq.s]

Three stable models: lparse -n 0 --partial pq.s|smodels

- $\mathcal{W}(\mathcal{P}) = (\emptyset, \emptyset)$ is the well-founded model, and a partial stable model,
- $\{p(a)\}$ whose 3-valued representation is $(\{p(a)\}, \{q(a)\})$ is a total stable model, and
- $\{q(a)\}$ whose 3-valued representation is $(\{q(a)\}, \{p(a)\})$ is also a total stable model.

Depending on the application

- the well-founded model tells that nothing is known.
- the two stable models tell what are the two possibilities that have to be considered (in a more complex scenario, this would already exclude some alternatives)
- underspecification: the two stable models tell that the user is allowed to state additional facts (according to his preferences).

12.1 Answer Set Programming

Different idea than

- Stratified Datalog[¬]: Query Answering
- Prolog: "Declarative" Prolog Programming the "search" is encoded into the SLD-resolution-tree.
- Rules as derivation: "if body holds, then derive head".

Answer Set Programming: Specify a problem declaratively and leave the reasoning to the ASP solver (from [EIK09]):

- Rules as assertions: "if body holds, then head holds".
- Allow disjunction and negation in the head.
- Possibility of modeling constraints;
- · Reasoning with incomplete information; and
- · Possibility of modeling preferences and priority.
- Spatial and temporal reasoning (here, the notorious Frame Problem is challenging).

672

SMODELS + LPARSE

- Call lparse -n 0 -d none [-partial] filename | smodels
- smodels requires "..." for strings,
- smodels does not accept the "_" don't-care underscore.
 Use X1, X2 etc. and constrain it by a domain predicate (see next slide).
- smodels does not accept decimal numbers only (positive and negative) integers
 - decimals would not allow a grounding of the program. (integers are only little better ...)
 - \Rightarrow thus, mondial.P cannot be used.

Grounding the Program in smodels: Domain Predicates

(note: important for writing programs)

- Computation of stable models is based on grounding the program (cf. generating the reduct of a program on Slide 631)
- For grounding the rules (i.e., generate all relevant ground instances of each rule), smodels internally looks for *"domain predicates"* whose extension can be precomputed by a simple Datalog[¬] subprogram of *P* without extended rules (cf. smodels Manual Sections 4.4.2 and 4.4.3):
 - union, intersection, join, set difference (with one negative literal!)
- every rule must contain at least one domain predicate atom.
- the ground instances of the domain predicates are precomputed and used for grounding.
 (cf. the example for the reduct of the win-move game generate only ground instances of win(X) :- move(X,Y), not win(Y) s.t. move(a,b) is in the EDB).
- If Iparse/smodels complains about

```
<line_nr>: weakly restricted rule: <....>.
    weakly restricted variables: <var>
```

introduce a domain predicate and use it in the rule (in the following: thing(X) with appropriate definition of thing).

674

DISJUNCTION REVISITED: STABLE MODELS

```
mainDish(X) :- meal (X,Y).
drink(Y) :- meal (X,Y).
vegetarian(X) :- mainDish(X), not nonvegetarian(X).
                                                         %% xor(veg, nonveg)
nonvegetarian(X) :- mainDish(X), not vegetarian(X).
porc(X) :- mainDish(X), nonvegetarian(X), not beef(X), not fish(X). %% xor (porc,beef,fish)
beef(X) :- mainDish(X), nonvegetarian(X), not porc(X), not fish(X).
fish(X) :- mainDish(X), nonvegetarian(X), not porc(X), not beef(X).
whitewine(Y) :- meal(X,Y), fish(X).
whitewine(Y) :- meal(X,Y), porc(X).
redwine(Y) :- meal(X,Y), beef(X).
wine(Y) :- drink(Y), redwine(Y).
                                                  %% wine = redwine u whitewine
wine(Y) :- drink(Y), whitewine(Y).
alcoholic(Y) :- drink(Y), wine(Y).
tomatojuice(Y) :- meal(X,Y), vegetarian(X).
meal(a,b).
nonvegetarian(a).
                                                [Filename: Datalog/meals.s and meals.P]
```

- consider the question: is *b* alcoholic?
- meal/2, mainDish/1 and drink/1 act as domain predicates.

Example (Cont'd)

- Three (total) stable models: *a* is either porc, beef or fish. In either case, white/red wine is served with it, thus alcoholic(*b*) holds.
- Exercise: give the AFP computation.
- well-founded model:

-
$$val_{\mathcal{W}(P)}(\mathsf{fish}(b)) = val_{\mathcal{W}(P)}(\mathsf{porc}(b)) = val_{\mathcal{W}(P)}(\mathsf{beef}(b)) = u$$
,

- $val_{\mathcal{W}(P)}(\mathsf{alcoholic}(b)) = u$
- note: XSB yields a=fish, not computing the well-founded model.

(cf. also formal example from Slide 666)

676

Logical Rules: Local and Global Semantics

- Wrt. logical rules, the concept of disjunction does not exist: there are several *isolated* rules that *derive* wine(X) (in Description Logics, wine would be a union class Wine = RedWine ⊔ WhiteWine).
- The *global* semantics of the well-founded model and of stable models is always based on the *local* semantics of rules.
- any application-specific semantics (= interpretation of the model) has to be defined outside of the LP framework.
- Consider I agreeing with the well-founded model up to val_I(fish(a)) = val_I(porc(a)) = val_I(beef(a)) = val_I(whitewine(b)) = val_I(redwine(b)) = u, but then setting val_I(wine(b)) = val_I(alcoholic)(b) = t: I ⊨ P, but I is not stable!
- Recall Lemma 11.2: " $W_P = (T, F)$ is the intersection of all 3-stable models of P". Above example: This may be smaller than the intersection of all 2-stable models!

APPLICATION-SPECIFIC INTERPRETATION OF LP NOTIONS

- consider all total stable models and
 - "cautious reasoning": take facts that are true/false in all of them. (results are models of P, but not necessary stable ones) (meals example: alcoholic(b))
 - "credulous reasoning": take facts that are true/false in one of them (they are possible - somebody reporting them may tell the truth) (meals example: whitewine(b), redwine(b), but tomatojuice(b) is definitely false)
- preference by the user
 - interpreted as underspecification:
 - choose a "desired" fact a that is undefined and consider only models that satisfy it,
 - add *a* to the program and run again
 - without negation in the head/denials (cf. Slide 683):
 one or more new 3-stable models exist
- systematic weight (lparse/smodels support weighted clauses)

678

DISJUNCTION IN RULE HEADS

(this syntax is buggy in smodels; see next page for (more expressive) alternative)

- rules of the form
 - $A_1 | \ldots | A_n := B_1, \ldots, B_m$

(recall: conjunction is expressed by n rules with the same body)

- · stable models in presence of disjunction are not necessarily minimal
- · check of minimality is again NP-complete
- · smodels yields all stable models
- smodels, Section 4.8.1
- invoke with --dlp
- smodels returns "Error in input" (lparse without | smodels accepts it)

```
a | b :- c.
```

```
c :- not d.
```

(Total) stable models:

```
d :- not c.
[Filename: Datalog/disj.s]
```

679

• $\{d\}, \{c, a\}, \{c, b\}, \{c, a, b\}.$

SMODELS: DISJUNCTION IN THE HEAD VIA CHOICE RULES

- extended rule head: $k \{a_1, \ldots, a_n\} m := body$
- *k* to *m* atoms of the head must be true if *body* is true.

```
mainDish(X) :- meal (X,Y).
drink(Y) :- meal (X,Y).
1{vegetarian(X),nonvegetarian(X)}1 :- meal(X,Y).
1{porc(X), beef(X), fish(X)}1 :- mainDish(X), nonvegetarian(X).
whitewine(Y) :- meal(X,Y), fish(X).
whitewine(Y) :- meal(X,Y), porc(X).
redwine(Y) :- meal(X,Y), beef(X).
wine(Y) :- drink(Y), redwine(Y).
wine(Y) :- drink(Y), whitewine(Y).
alcoholic(Y) :- drink(Y), wine(Y).
tomatojuice(Y) :- meal(X,Y), vegetarian(X).
meal(a,b).
nonvegetarian(a).
```

680

Stable Models – Example

Consider the following program (cf. Slide 635):

1{p(a), q(a)}1. p(a).

[Filename: Datalog/pporq-choice.s]

- The program has only one *total* stable model: {*p*(*a*)}. (which corresponds to the 3-valued ({*p*(*a*)}, {*q*(*a*)}.)
- The 3-valued interpretation ({p(a)}, ∅) (Stable Model: p(a) p'(a) q'(a)) is also considered a (partial) stable model (!) [Bug or not bug?]

EXPLICIT NEGATION

- well-founded and stable semantics are still based on default negation. non-monotonic: adding some positive atom is always allowed and may make before conclusions invalid (and add others).
- explicit negation:
 - $\neg p(a_1, \ldots, a_n)$ as negative facts,
 - $\neg p(X_1, \ldots, X_n)$:- ... in rule heads.
- Explicit negation is monotonic. "Additional" positive information wrt. such atoms would make the program inconsistent.
- applications:
 - in diagnosis systems to explicitly derive negative knowledge,
 - for expressing integrity constraints.
- XSB: WSFX package, XSB Manual Part II.
- smodels: only integrity constraints via *denials* (see next slide).

682

EXPLICIT NEGATION VIA DENIALS

A *denial* is a constraint that forbids certain database states (DB: integrity constraints can be formulated as denials)

• Consider a "rule"

:- p.

Its semantics is "if p is true, then the empty clause is true", i.e., then, "false" is true.

• means "p must not be true".

```
:- p(a).
q(a) :- not p(a).
p(a) :- not q(a).
```

[Filename: Datalog/porq-denial.s]

- the program has only one stable model, $\{q(a)\}$. It is total.
- note: XSB does not care for such rules (they would be useless there since XSB computes only one model).

Example: Italians Revisited

The italian-vs-english ontology from Slide 546 can be specified via choice rules (and implicit) denials (line 1: either italian or english allowed):

<pre>0{ italian(X), english(X) }1 :- person(X),</pre>	thing(X).
<pre>person(X) :- italian(X),</pre>	thing(X).
<pre>person(X) :- english(X),</pre>	thing(X).
<pre>1{ lazy(X), latinlover(X) }1 :- italian(X),</pre>	thing(X).
<pre>italian(X) :- lazy(X),</pre>	thing(X).
<pre>italian(X) :- latinlover(X),</pre>	thing(X).
O{ gentleman(X), hooligan(X) }2 :- english(X),	thing(X).
<pre>english(X) :- gentleman(X),</pre>	thing(X).
<pre>english(X) :- hooligan(X),</pre>	thing(X).
<pre>gentleman(X) :- latinlover(X),</pre>	thing(X).
italian(e).	
thing(e).	

[Filename: Datalog/italians-english.s]

- do not query for ?- lazy(e) , but inspect the stable model(s).
- there is a single (total) stable model where lazy(e) holds.

684

SMODELS: MULTIPLE MODELS

• Motivated by the "Ascending, Descending" graphics by M.C.Escher http://en.wikipedia.org/wiki/Ascending_and_Descending

```
corner(1..4). % set of corners
higher(1,2).
1{ higher(1,2), higher(1,3), higher(1,4) }1.
1{ higher(2,1), higher(2,3), higher(2,4) }1.
1{ higher(2,1), higher(2,3), higher(2,4) }1.
1{ higher(3,1), higher(3,2), higher(3,4) }1.
1{ higher(4,1), higher(4,2), higher(4,3) }1.
:- higher(4,1), higher(4,2), higher(4,3) }1.
:- higher(X,X), corner(X). % irreflexive
:- higher(X,X), corner(X). % orner(Y). % asymmetric
% inverse functional
:- higher(Y,X), higher(Z,X), corner(X), corner(Y), corner(Z), Y != Z.
% :- higher(X,Y), higher(X,Z), corner(X), corner(Y), corner(Z), Y != Z.
```

[Filename: Datalog/escherstairs.s]

- two possibilities = two models
- recall Semantic Web: only answers what holds in all models

SMODELS: PLANNING

Give a specification *P* of the workflow including constraints:

• if at least one total stable model *S* exists, the specification including the constraints is satisfiable.

 \boldsymbol{S} describes the plan that must be followed.

- if several total stable model exist, each one represents a possible execution. Different plans mean that choicepoints during the execution exist.
 - they can be decided a priori: add the intended atoms to P:
 - * there is at least one stable model, but maybe still several ones.
 - ... or decide them during execution of the workflow (e.g. to be able to react upon external influences).

686

Planning Example: The Farmer's Puzzle

A farmer, travelling to the market with his dog, a goat, and a cabbage. He has to cross a small river, where a boat can be used.

- When using the boat, he can transport only one item.
- He can cross the river as often as he wants.
- When the dog stays on the same side as the goat, and the farmer is not there, the dog will kill and eat the goat.
- When the goat stays on the same side as the cabbage, and the farmer is not there, the goat will eat the cabbage.

Is it possible for the farmer to bring all items to the other side? If yes, how?

```
Example (Cont'd)
state(1..8).
                 % estimate the number of necessary states.
side(1). side(r).
is(farmer,1,1).
                    % farmer is on the left side in state 1 (with all items)
thing(cabbage). thing(goat). thing(dog).
is(X,1,1) := thing(X).
otherside(X,Y) :- side(X), side(Y), X != Y.
O{ transport(cabbage,N), transport(goat,N), transport(dog,N) }1 :- state(N), not finished(N).
:- transport(X,N), is(farmer,S1,N), is(X,S2,N), S1 != S2,
   thing(X), state(N), side(S1), side(S2).
is(X,S2,M) :- is(X,S1,N), thing(X), otherside(S1,S2), transport(X,N), M = N+1, not finished(N)
   state(N), side(S1).
is(X,S1,M) := is(X,S1,N), thing(X), not transport(X,N), M = N+1, not finished(N),
                           %% the "frame axiom"
   state(N), side(S1).
is(farmer,S2,M) :- is(farmer,S1,N), otherside(S1,S2), M = N+1, not finished(N),
   state(N), side(S1).
:- is(cabbage,S,N), is(goat,S,N), not is(farmer,S,N), state(N), side(S).
:- is(goat,S,N), is(dog,S,N), not is(farmer,S,N),
                                                        state(N), side(S).
finished(N) :- is(cabbage,r,N), is(goat,r,N), is(dog,r,N),
                                                                  state(N).
finished(M) :- finished(N), M = N+1,
                                                                   state(N).
:- not finished(8).
                                                [Filename: Datalog/farmer.s]
```

688

Example (Cont'd)

Two stable models:

- first carry the goat to the other side (r) (it must not be left with the dog or with the cabbage).
- 2. go back,
- 3. bring either the dog or the cabbage to the other side,
- 4. go back with the goat,
- 5. bring the cabbage or the dog (one is still there) to the other side,
- 6. go back,
- 7. take the goat and bring it to the right bank again,
- 8. continue traveling to the market.
- \Rightarrow Step 3 is a choicepoint.

SMODELS: SUDOKU SOLVER % example sudoku content from (german) wikipedia p(2,9,3). p(4,8,1). p(5,8,9). p(6,8,5). p(3,7,8). p(8,7,6). p(1,6,8). p(5,6,6). p(1,5,4). p(4,5,8). p(9,5,1). p(5,4,2). p(2,3,6). p(7,3,2). p(8,3,8). p(4,2,4). p(5,2,1). p(6,2,9). p(9,2,5). p(8,1,7). % general sudoku rules (x = cols, y = rows) col(1..9). row(1..9). num(1..9). % samesquare expresses the 3x3 subsquares: [Filename: Datalog/sudoku.s] samesq(1,2). samesq(1,3). samesq(2,3). (cf. Sudoku from Slide 584) samesq(4,5). samesq(4,6). samesq(5,6). samesq(7,8). samesq(7,9). samesq(8,9). samesq(B,A) :- samesq(A,B), num(A), num(B). 1{p(X,Y,1),p(X,Y,2),p(X,Y,3),p(X,Y,4),p(X,Y,5),p(X,Y,6),p(X,Y,7),p(X,Y,8),p(X,Y,9)}1 :- col(Y), row(X). :- p(X,Y1,N), p(X,Y2,N), col(X), row(Y1), row(Y2), num(N), Y1!=Y2. :- p(X1,Y,N), p(X2,Y,N), col(X1), col(X2), row(Y), num(N), X1!=X2. :- p(X1,Y1,N), p(X2,Y2,N), col(X1), col(X2), row(Y1), row(Y2),num(N), samesq(X1,X2), samesq(Y1,Y2), X1 + 10 * Y1 != X2 + 10 * Y2.

690

Aside: Another Sudoku

 for most strategy-based solvers it is "unsolvable", requires "trial and error" (which is actually backtracking)



```
Aside: Code for another Sudoku - easier encoding of input
% another sudoku which is unsolvable by rule-based reasoners:
r(9, 6,0,0,0,0,2,0,0,8).
r(8, 0,0,7,0,0,0,0,3,0).
r(7, 0, 4, 0, 1, 0, 0, 9, 0, 0).
r(6, 0,8,0,9,0,0,0,0,2).
r(5, 0,0,0,0,0,7,0,6,0).
r(4, 0,0,3,0,5,0,0,0,0).
r(3, 0,0,1,0,0,3,0,0,4).
r(2, 0,5,0,0,0,0,7,0).
r(1, 9,0,0,0,6,0,0,0).
col(1..9). row(1..9).
                         num(1..9). numx(0..9).
                                                                  [Filename: Datalog/sudoku2.s]
9{q(1,Y,X1), q(2,Y,X2), q(3,Y,X3), q(4,Y,X4), q(5,Y,X5),
               q(6,Y,X6), q(7,Y,X7), q(8,Y,X8), q(9,Y,X9)}9
  :- r(Y,X1,X2,X3,X4,X5,X6,X7,X8,X9), row(Y),
    numx(X1), numx(X2), numx(X3), numx(X4), numx(X5), numx(X6), numx(X7), numx(X8), numx(X9).
p(X,Y,N) :- q(X,Y,N), col(X), row(Y), num(N). %% Os are unknown cells
% general sudoku rules as before ...
% samesquare expresses the 3x3 subsquares:
samesq(1,2). samesq(1,3). samesq(2,3).
samesq(4,5). samesq(4,6). samesq(5,6).
samesq(7,8). samesq(7,9). samesq(8,9).
samesq(B,A) :- samesq(A,B), num(A), num(B).
                                             692
```

COMMENTS AND LINKS ON ASP AND SUDOKU SOLVING

- None of the rules is "constructive" in the sense of "position (x, y) must be n_1 if ...", or "position (x, y) must be n_1 of n_2 if ..."
- the description strongly relies on the denials and the solver must find out what is not forbidden.
- Sudoku is a typical Constraint Satisfaction Problem; ASP is a certain form of Constraint Solving.
 See e.g. https://en.wikipedia.org/wiki/Constraint_satisfaction_problem.
- Sudoku solved by an explicit Constraint Propagation algorithm in python:

http://norvig.com/sudoku.html by Peter Norvig, a well-known AI scientist.

SMODELS: FURTHER EXAMPLES AND PUZZLES

- the smodels documentation (Section 6.1) contains
 - the Graph 3-Coloring problem (sudoku can also be encoded as graph coloring),
 - some logical puzzles.
- Exercise: encode the Fish Puzzle (see Web page) in ASP and let smodels solve it.

"Prove" $P \models \varphi$

- Stable models:
 - definition (cf. Slide 656) is based on grounding P with the active domain.
 - \Rightarrow Problem solving for concrete cases answer queries, look for ground atoms.
- It is only possible to show that $S \models \varphi$ for all *stable* models S of P:
- Show $P \models_{s} \varphi$ (1st Alternative):
 - generate all stable models S_1, \ldots, S_n .
 - for each of them check whether $S_i \models \varphi$ (if not, it is a witness for a counterexample)
- Show $P \models_{s} \varphi$ (2nd Alternative):
 - encode $\neg \varphi$ in a program P',
 - run smodels on $P \cup P'$,
 - if there is a stable model, then, $P \not\models_s \varphi$ (and, again, a witness for a counterexample has been found).

694

EXAMPLE: PARRICIDES IN GREEK MYTHODOLOGY

(from ESWC'07 SPARQL tutorial by Marcelo Arenas et al)

A parricide is a person who killed his/her father.

[Filename: Datalog/parricide.s]

```
1{ parricide(X), nonParricide(X) }1 :- person(X).
person(iokaste). nonParricide(iokaste).
hasChild(iokaste, oedipus).
person(oedipus). parricide(oedipus).
marriedto(oedipus, iokaste).
                               %% irrelevant, but the reason why he became prominent
hasChild(oedipus, perineikes).
person(perineikes).
                        %% unknown whether parricide or not.
hasChild(perineikes, thesandros).
person(thesandros). nonParricide(thesandros).
parentOfParricide(X) :- hasChild(X,Y), parricide(Y).
parentOfNonParricide(X) :- hasChild(X,Y), nonParricide(Y).
parentOfParricideGrandparentOfNonParricide(X) :-
   parentOfParricide(X), hasChild(X,Y), parentOfNonParricide(Y).
existsPoPGoNP :- parentOfParricideGrandparentOfNonParricide(X), person(X). %% => t/f
```

Does $P \models_S \exists X : parentOfParricideGrandparentOfNonParricide(X)?$

• two possibilities: either lokaste or Oedipus.

FOL ENTAILMENT/PROOFS VS. STABLE MODELS/ASP

Consider again the italian-vs-english ontology from Slides 546 and 684:

- FOL/Tableaux: prove Spec_{ItalEngl} ⊨ ∀x : italian(x) → lazy(x) (without considering any ground instance)
- ASP: show that in all stable models of italians-english.s, lazy(e) holds.
- this conclusion is weaker than the one for FOL.
 - e is a "typical" instance of an italian, but
 - recall that Stable Models reasoning is nonmonotonic more knowledge about *e* could invalidate this conclusion.

696

MONOTONIC VS. NONMONOTONIC REASONING

• FOL:

 $(\forall x : bird(x) \land \neg penguin(x) \rightarrow flies(x)) \land bird(tweety) \not\models flies(tweety)$ $(\forall x : bird(x) \land \neg penguin(x) \rightarrow flies(x)) \land bird(tweety) \not\models \neg flies(tweety))$

FOL reasoning does not entail any anything about tweety – Open World.

- $(\forall x : bird(x) \land \neg penguin(x) \rightarrow flies(x)) \land bird(tweety) \land penguin(tweety) \models \neg flies(tweety))$ $(\forall x : bird(x) \land \neg penguin(x) \rightarrow flies(x)) \land bird(tweety) \land \neg penguin(tweety) \models flies(tweety))$
- FOL is monotonic. More knowledge, more conclusions, no conclusions can/must ever be withdrawn.
- it is not possible to *conclude* things that cannot be actually proven (and that may have to be withdrawn later).

```
Monotonicity vs. Nonmonotonicity (cont'd)
• ASP:
     flies(X) :- bird(X), not penguin(X).
     bird(tweety). [Filename: Datalog/tweety.s]
Stable Model: bird(tweety) flies(tweety) bird'(tweety) flies'(tweety)
     flies(X) :- bird(X), not penguin(X).
     bird(tweety).
     penguin(tweety). [Filename: Datalog/tweety2.s]
Stable Model: bird(tweety) penguin(tweety) bird'(tweety) penguin'(tweety)
```

```
698
```

Monotonicity vs. Nonmonotonicity (cont'd)

This can be used to encode general concepts in nonmonotonic reasoning

- by default, if p(x) holds, and there is no further information, then usually q(x) can be assumed.
- if p(x) holds, and q(x) is consistent with the knowledge, conclude q(x):
- "Circumscription" (J. McCarthy, "Circumscription A form of non-monotonic reasoning". Artificial Intelligence 13: 27-39, April 1980).

```
flies(X) :- bird(X), not abnormal(X).
abnormal(X) :- penguin(X).
bird(tweety).
[Filename: Datalog/tweety-circ.s]
```

Stable Model: bird(tweety) flies(tweety) bird'(tweety) flies'(tweety)

- In (T, F)-notation: ({bird(tweety), flies(tweety)}, {penguin(tweety), abnormal(tweety)})
- Note that ({bird(tweety), penguin(tweety), abnormal(tweety)}, {flies(tweety) }) is also a model of *P*, but it is not stable.
 If learning that penguin(tweety) holds, this model would become (the only) stable one.

12.2 An Application: Semantics of Referential Actions in SQL

Consider again the problem of ambiguous semantics of referential actions from Slide 236:

Country							
Name	Code	Capital	Province				
Germany	Ď	Berlin	Berlin				
United States	US	Washington	Distr.Col.	CI	SCADE	Province	e
	<u> </u>				Name	Country	Capital
	SET	NULL	CASCADE		Berlin	D	Berlin
City				Distr.Col.	US	Washington	
Name	Country	Province					
Berlin	D	В					
Washington	USA	Distr.Col.		DEL	ETE FROM C	ountry	
			WHERE Code='D'				

700

SQL Standard gives a hard-to-understand *procedural* specification of referential actions. Database Systems implemented only ON DELETE CASCADE (as optional alternative to ON DELETE NO ACTION) for a long time (late 90s) Nondeclarative semantics if ON DELETE SET NULL or ON UPDATE CASCADE are implemented. e.g. Oracle 11: the most recently defined (more exactly: activated) referential action is executed first. combination with transactions and PL/SQL and triggers becomes complex.

Concepts

- Intuitive concept of "Event-Condition-Action-Rules" ("ECA Rules"): ON DELETE (of referenced tuple) CASCADE (update to referencing tuple(s)
- can be read as a declarative specification how integrity is to be maintained:
 "Whenever the set U of updates includes the deletion of a referenced tuple wrt. a referential integrity constraint S.B → R.A, the cascaded update of the referencing tuple(s) must also be contained in U. (etc. for other referential actions)"
- ⇒ Set-oriented characterization of all updates that "complete" a transaction wrt. referential integrity maintenance.

702

... from a declarative point of view, the semantics should be easy, and it *must* be unambiguous. This lead us to playing around with Datalog (and Statelog) around Easter 1996:

Publications

The following papers are accessible via http://dblp.uni-trier.de/ (and partially via the DBIS Publications Web pages):

- B. Ludäscher, W. May und J. Reinert. Towards a Logical Semantics for Referential Actions in SQL. In *Proc. Intl. Workshop on Foundations of Models and Languages for Data and Objects: Integrity in Databases (FMLDO'96)*, Dagstuhl Castle, Germany, 1996.
- B. Ludäscher, W. May und G. Lausen. Referential Actions as Logical Rules. In *Proc. ACM Symposium on Principles of Database Systems (PODS'97)*, pp. 217–224, 1997.
- B. Ludäscher und W. May. Referential Actions: From Logical Semantics to Implementation. In *Proc. Intl. Conference on Extending Database Technology (EDBT'98)*, Springer LNCS 1377, pp. 404-418, 1998.
- W. May und B. Ludäscher. Understanding the Global Semantics of Referential Actions using Logic Rules. In *ACM Transactions on Database Systems (TODS)*, 27(4):343–397, 2002.

12.2.1 Straightforward Logical Semantics: Encoding as Rules

• consider only ON DELETE CASCADE/SET NULL:

```
% prov(Country) refs country(code) on delete cascade
del_province(PN,C,PPop,PA,PCap,PCapProv) :- del_country(N,C,Cap,CapP,A,P),
    province(PN,C,PPop,PA,PCap,PCapProv).
% city(Country) refs country(code) on delete set null
upd_city(CN,C,CP,CPop,Lat,Long,E1,CN,null,CP,CPop,Lat,Long,E1) :-
    del_country(N,C,Cap,CapP,A,P), city(CN,C,CP,CPop,Lat,Long,El).
% city(Country, Province) refs province(name, country) on delete cascade
del_city(CN,C,PN,CPop,Lat,Long,El) :- del_province(PN,C,PPop,PA,PCap,PCapProv),
    city(CN,C,PN,CPop,Lat,Long,El).
inconsistent :- del_city(CN,C,CP,CPop,Lat,Long,El),
                 upd_city(CN,C,CP,CPop,Lat,Long,E1,CN2,C2,CP2,CPop2,Lat2,Long2,E12).
country("Germany", "D", "Berlin", "Berlin", 356910, 83536115).
province("Berlin","D",3472009,889,"Berlin","Berlin").
city("Berlin","D","Berlin",3472009,13,52,null).
del_country("Germany", "D", "Berlin", "Berlin", 356910, 83536115).
% ?- inconsistent.
                                                             [Filename: Datalog/refint.s]
```

• cascaded updates and "inconsistent" are true.

704

Deletions: Encoding as Rules

- ON DELETE/UPDATE NO ACTION:
 - if there is a referencing tuple that is not deleted (or modified to reference another parent) in the same transaction, then the update is not allowed, e.g., in the reference Organization(City,Country,Province) → City(City,Country,Province) ON DELETE NO ACTION ON UPDATE CASCADE
 - a city where an organization has its headquarter cannot be deleted (i.e., when the city is merged with another one, the value must also be changed in the referenced organization tuple in the same transaction),
 - * if a city where an organization has its headquarter is renamed or its province changes, then, the update is cascaded to the headquarter foreign key.
- \Rightarrow all potential (cascaded) updates during the transaction must be considered.
 - ext_ACTION ("external"): the updates issued by the user/by the program.
 - pot_ACTION ("potential"): all updates issued by the user/by the program or resulting from these by any referential action.

12.2.2 Deletions: Encoding as Rules

• Collect all potential updates that are triggered by the external operations:

• Consider only deletions and ON DELETE CASCADE/NO ACTION.

```
706
```

Deletions: Encoding as Bules	
pot_del_organization(U,N,Ci,Co,P,E) :- e	xt_del_organization(U,N,Ci,Co,P,E),
organization(U,N,Ci,Co,P,E).	
% refs from isMember to Country and Orga	nization: ON DELETE CASCADE.
<pre>pot_del_isMember(C,O,T) :- pot_del_count</pre>	ry(N,C,Cap,CapP,A,Pop),
<pre>pot_del_isMember(C,0,T) :- pot_del_count</pre>	ry(N,C,Cap,CapP,A,Pop),
<pre>pot_del_isMember(C,0,T) :- pot_del_count</pre>	<pre>ry(N,C,Cap,CapP,A,Pop), ization(0,N,Ci,Co,P,E),</pre>

Deletions: Encoding as Rules

- Organization(City,Country,Province) → City(City,Country,Province) ON DELETE NO ACTION ON UPDATE CASCADE
- block deletions/updates if ON UPDATE NO ACTION and child tuple remains,
- propagate blocking upwards through CASCADEs.

```
blk_del_city(Ci,Co,P,CPop,Lat,Long,El) :- pot_del_city(Ci,Co,P,CPop,Lat,Long,El),
organization(0,N,Ci,Co,P,E), rem_organization(0,N,Ci,Co,P,E).
rem_organization(0,N,Ci,Co,P,E) :- organization(0,N,Ci,Co,P,E),
not del_organization(0,N,Ci,Co,P,E). %%% del not yet defined
blk_del_province(P,C,PPop,PA,PCap,PCapProv) :- pot_del_city(CN,C,P,CPop,Lat,Long,El),
blk_del_city(CN,C,P,CPop,Lat,Long,El), pot_del_province(P,C,PPop,PA,PCap,PCapProv).
blk_del_country(N,C,Cap,CapP,A,Pop) :- pot_del_province(P,C,PPop,PA,PCap,PCapProv),
blk_del_province(P,C,PPop,PA,PCap,PCapProv), pot_del_country(N,C,Cap,CapP,A,Pop).
```

```
708
```

Deletions: Encoding as Rules

- (if any update is blocked do nothing).
- execute (and appropriately cascade) all external updates that are not blocked.

```
del_country(N,C,Cap,CapP,A,Pop) :- ext_del_country(N,C,Cap,CapP,A,Pop),
    country(N,C,Cap,CapP,A,Pop), not blk_del_country(N,C,Cap,CapP,A,Pop).
del_province(P,C,PPop,PA,PCap,PCapProv) :- del_country(N,C,Cap,CapP,A,Pop),
    province(P,C,PPop,PA,PCap,PCapProv).
del_city(CN,C,P,CPop,Lat,Long,El) :- del_country(N,C,Cap,CapP,A,Pop),
    city(CN,C,P,CPop,Lat,Long,El).
del_city(CN,C,P,CPop,Lat,Long,El) :- del_province(P,C,PPop,PA,PCap,PCapProv),
    city(CN,C,P,CPop,Lat,Long,El).
del_isMember(C,O,T) :- del_country(N,C,Cap,CapP,A,P), isMember(C,O,T).
del_organization(0,N,Ci,Co,P,E) :- ext_del_organization(0,N,Ci,Co,P,E),
    organization(0,N,Ci,Co,P,E), not blk_del_organization(0,N,Ci,Co,P,E).
del_isMember(C,0,T) :- del_organization(0,N,Ci,Co,P,E), isMember(C,0,T).
[Filename: Datalog/refint4.s]
 • Dependency graph: ext \rightarrow pot \rightarrow blk
                                                              del
                                                    rem
```

Deletions Example: delete Germany (not referenced)

```
country("Germany","D","Berlin","Berlin",356910,83536115).
province("Berlin","D",3472009,889,"Berlin","Berlin").
city("Berlin","D","Berlin",3472009,13,52,null).
organization("EU","European Union","Brussels","B","Brabant","1992-02-07").
isMember("D","EU","member").
ext_del_country("Germany","D","Berlin","Berlin",356910,83536115).
% lparse -n 0 refint1.s refint2.s refint3.s refint4.s refint-del-d.s| smodels
```

```
[Filename: Datalog/refint-del-d.s]
```

In this case, there is only one stable model (i.e., it coincides with the well-founded model) which is total:

```
pot_del_country("Germany", "D", "Berlin", "Berlin", 356910,83536115)
pot_del_province("Berlin", "D", 3472009,889, "Berlin", "Berlin")
pot_del_city("Berlin", "D", "Berlin", 3472009,13,52,null)
pot_del_isMember("D", "EU", "member")
del_country("Germany", "D", "Berlin", "Berlin", 356910,83536115)
del_province("Berlin", "D", 3472009,889, "Berlin", "Berlin")
del_city("Berlin", "D", "Berlin", 3472009,13,52,null)
del_city("Berlin", "D", "Berlin", 3472009,13,52,null)
rem_organization("EU", "European Union", "Brussels", "B", "Brabant", "1992-02-07")
```

710



Deletions Example - delete Belgium and the EU

ext_del_country("Belgium", "B", "Brussels", "Brabant", 30510, 10170241). ext_del_organization("EU", "European Union", "Brussels", "B", "Brabant", "1992-02-07"). country("Belgium","B","Brussels","Brabant",30510,10170241). city("Brussels", "B", "Brabant", 951580, null, null, null). province("Brabant", "B", 2253794, 3358, "Brussels", "Brabant"). organization("EU", "European Union", "Brussels", "B", "Brabant", "1992-02-07"). isMember("B","EU","member"). % lparse -n 0 refint1.s refint2.s refint3.s refint4.s refint-del-b2.s| smodels [Filename: Datalog/refint-del-b2.s] Again, a total unique stable model = well-founded model: ext_del_country("Belgium", "B", "Brussels", "Brabant", 30510, 10170241) ext_del_organization("EU","European Union","Brussels","B","Brabant","1992-02-07") pot_del_ [...] del_country("Belgium", "B", "Brussels", "Brabant", 30510, 10170241) del_city("Brussels", "B", "Brabant", 951580, null, null, null) del_province("Brabant", "B", 2253794, 3358, "Brussels", "Brabant") del_isMember("B","EU","member") del_organization("EU", "European Union", "Brussels", "B", "Brabant", "1992-02-07")

712

Deletions Example with NO ACTION

 Change the reference from City to Province from CASCADE to NO ACTION: (in refint1.s and refint4.s)

```
pot_del_country(N,C,Cap,CapP,A,Pop) :- ext_del_country(N,C,Cap,CapP,A,Pop),
        country(N,C,Cap,CapP,A,Pop).
% Province(Country) refs Country(code) on delete cascade
pot_del_province(P,C,PPop,PA,PCap,PCapProv) :- pot_del_country(N,C,Cap,CapP,A,Pop),
        province(P,C,PPop,PA,PCap,PCapProv).
% City(Country) refs Country(code) on delete cascade
pot_del_city(CN,C,P,CPop,Lat,Long,El) :-
    pot_del_country(N,C,Cap,CapP,A,Pop),
    city(CN,C,P,CPop,Lat,Long,El).
% City(Country, Province) refs Province(name, country) on delete no action <<<<<<<
blk_del_province(P,C,PPop,PA,PCap,PCapProv) :-
  pot_del_province(P,C,PPop,PA,PCap,PCapProv),
  city(CN,C,P,CPop,Lat,Long,El), rem_city(CN,C,P,CPop,Lat,Long,El).
rem_city(CN,C,P,CPop,Lat,Long,El) :- city(CN,C,P,CPop,Lat,Long,El),
                               not del_city(CN,C,P,CPop,Lat,Long,El).
[Filename: Datalog/refint1b.s]
```

Deletions: Encoding as Rules

[Filename: Datalog/refint4b.s]

 using pot_del is sometimes redundant, and only required for providing smodels with a domain predicate.

714

Deletions: The Resulting Models

% lparse -n 0 refint1b.s refint2.s refint3.s refint4b.s refint-del-d.s| smodels

• 3 stable models, 2 of them total, one partial (= well-founded model).

```
ext_del_country("Germany","D","Berlin","Berlin",356910,83536115)
pot_del_country("Germany","D","Berlin","Berlin",356910,83536115)
pot_del_province("Berlin","D",3472009,889,"Berlin","Berlin")
pot_del_isMember("D","EU","member")
del_province("Berlin","D",3472009,889,"Berlin","Berlin")
del_country("Germany","D","Berlin","Berlin",356910,83536115)
del_city("Berlin","D","Berlin",3472009,13,52,null)
del_isMember("D","EU","member")
ext_del_country("Germany","D","Berlin","Berlin",356910,83536115)
pot_del_country("Germany","D","Berlin","Berlin",356910,83536115)
pot_del_country("Germany","D","Berlin","Berlin",356910,83536115)
pot_del_country("Germany","D","Berlin","Berlin",356910,83536115)
pot_del_country("Germany","D","Berlin","Berlin",356910,83536115)
pot_del_country("Germany","D","Berlin","Berlin",356910,83536115)
pot_del_country("Germany","D","Berlin","Berlin",356910,83536115)
pot_del_country("Germany","D","Berlin","Berlin",356910,83536115)
pot_del_country("Germany","D","Berlin","Berlin","Berlin",356910,83536115)
pot_del_[...]
blk_del_country("Germany","D","Berlin","Berlin","Berlin",356910,83536115)
blk_del_province("Berlin","D",3472009,889,"Berlin","Berlin","Berlin")
rem_city("Berlin","D","Berlin",3472009,13,52,null)
```

• in the partial stable model (=the well-founded model), all pot_del are true, all blk_del and all del are undefined.

Deletions: Interpreting the Resulting Models

3 stable models:

- 1. the well-founded, partial one: all pot_del are true, the blk_del and del are undefined.
- two total stable ones:
 - all pot_del are true, the del are true, and the blk_del are false (since the reason for blk_del_prov(...) is deleted).
 - 3. all pot_del are true, the blk_del are true, and the del are false (since the deletion of the province is not allowed due to blocking).

Application-Specific Priorities (cf. EDBT paper)

- the "intended" one is the stable model (2) that gives priority to deletions against blockings.
- including game-theoretic interpretation:
 - "del_p(\bar{x})" is won if deletion is possible
 - counter-moves: "how?" and "what about this referencing tuple $q(\bar{y})$ ",
 - justification "cascaded from "del_r(\bar{z})" and "claim: del_q(\bar{y})",
 - infinite games (cycling around via deleted blocking tuples) are won for the deleter.
 - the well-founded model can be used \rightarrow polynomial.

716

Deletions: Encoding as Rules

- Sets of (external) delete requests are monotonic:
 Let del(D) denote the actual set of (cascaded) deletions on the database.
- $del(D_1 \cup D_2) = del(D_1) \cup del(D_2),$
- If D₁ and D₂ are admissible (wrt. NO ACTION), then D₁ ∪ D₂ is admissible (but not vice versa, recall the "Belgium" example – D₁ ∪ D₂ is admissible even though D₁ alone is not admissible).
- with CASCADE and SET NULL, conflicts can arise;
- with DELETE+CASCADE/SET NULL and UPDATE even more conflicts can arise.

12.2.3 Updates: Encoding as Rules

- with updates, the modeling is more involved:
 - updates can create new foreign keys,
 - usually such updates are cascaded from the appropriate parent,
 - but overlapping FKs induce interferences with other K/FKs.
 - Consider S.X \rightarrow R.Y ON UPDATE NO ACTION and r(a), r(b) and s(a). A transaction that modifies $r(a) \rightarrow r(c)$ and $s(a) \rightarrow s(b)$ is admissible.
 - \Rightarrow not only tuple-based, but key-foreign-key-based.
 - different cascaded modifications can be applied at the same time to a tuple.
- Recall:
 - SET NULL cannot create new foreign keys null values cannot violate any SQL integrity constraint (except NOT NULL).
 - actual conflicts in a "diamond" from a single update can only result from CASCADE and SET NULL since then *different* changes are applied.
- the approach must cover the general "worst case", not only "intuitive" cases.

718

Updates: Encoding as Rules

- for every key and foreign key: pot_chg_R_K_1...K_k(X_1,...,X_n,Y_1,...,Y_k) and chg_R_K_1...K_k(X_1,...,X_n,Y_1,...,Y_k) (change f/key attributes K_1,...,K_k of tuple R(X_1,...,X_n) to Y_1,...,Y_k).
- propagation for every FK/K reference (ON UPDATE CASCADE): pot_prp_R_P_R_C_F₁...F_k(X₁,...,X_n,Y₁,...,Y_k) (propagate update from R_P's keys to FK F₁,...,F_k of tuple R_C(X₁,...,X_n)).
- user updates: projection to the keys and foreign keys (K₁,...,K_k) of R: pot_prp_ext_R_K₁...K_k(X₁,...X_n,Y_{i1},...,Y_{ik}) :ext_mod_R(X₁,...,X_n,Y₁,...,Y_n), (Y_{i1},...,Y_{ik}) != (X_{i1},...,X_{ik}).
- collect propagated changes to keys/foreign keys (overlappings!): Simplified pattern: Consider two "incoming" propagations from $R_{P_1}.A \rightarrow R_C.K_1$ and $R_{P_1}.B \rightarrow R_C.K_2$ concern the key (K_1, K_2) of R_C : pot_chg_R_C_K_1,K_2(X_1,...,X_n,Y_1,Y_2) :pot_prp_R_{P_1}_R_C_K_1(X_1,...,X_n,Y_1), pot_prp_R_{P_2}_R_C_K_2(X_1,...,X_n,Y_2), $(Y_1,Y_2) != (X_{K_1},X_{K_2}).$

(for the fully general rule see (CH_1) in the TODS paper)

Updates: Encoding as Rules

Changes of Primary Keys $R_P(K_1, ..., K_k)$ are then handled according to the referential actions of their "child tuples"

• $R_C(F_1, \ldots, F_k)$ REFERENCES $R_P(K_1, \ldots, K_k)$ ON UPDATE NO ACTION: blk chg R_P $K_1, ..., K_k(X_1, ..., X_n, Y_1, ..., Y_k)$:pot_chg_R_P_K₁,...,K_k(X₁,...,X_n,Y₁,...,Y_k), rem_refd_R_P_R_C_F₁...F_k(Y₁,...,Y_k). • $R_C(F_1, \ldots, F_k)$ REFERENCES $R_P(K_1, \ldots, K_k)$ ON UPDATE CASCADE: pot_prp_ $R_P_R_C_F_1...F_k(Z_1,...,Z_n,Y_1,...,Y_k)$:pot_chg_R_P_K_1,...,K_k(X_1,...,X_n,Y_1,...,Y_k), $\pi[\mathsf{F}_1,\ldots,\mathsf{F}_k](\mathsf{Z}_1,\ldots,\mathsf{Z}_n) = \pi[\mathsf{K}_1,\ldots,\mathsf{K}_k](\mathsf{X}_1,\ldots,\mathsf{X}_n).$ and (block propagation if change of child is blocked) blk_prp_R_P_R_C_F₁...F_k(X₁,...,X_n,Y₁,...,Y_k) :pot prp $R_P R_C F_1...F_k(X_1,...,X_n,Y_1,...,Y_k)$, blk chg R_C $\mathsf{F}_1,\ldots,\mathsf{K}_k(\mathsf{X}_1,\ldots,\mathsf{X}_n,\mathsf{Y}_1,\ldots,\mathsf{Y}_k)$ and (block parent change if propagation to some child is blocked) blk_chg_R_P_K₁,...,K_k(X₁,...,X_n,Y₁,...,Y_k), pot chg R_P $K_1, ..., K_k(X_1, ..., X_n, Y_1, ..., Y_k)$, blk_prp_R_P_R_C_F₁...F_k(Z₁,...,Z_n,Y₁,...,Y_k), $\pi[F_1,\ldots,F_k](Z_1,\ldots,Z_n) = \pi[K_1,\ldots,K_k](X_1,\ldots,X_n).$

720

Updates: Encoding as Rules

Further rules (see TODS paper):

- when a key value remains referenced (child not deleted, not "modified away"),
- when a key value gets newly referenced (insert, "modified towards"),
- when a key value gets newly referencable (insert, "modified towards"),
- when a change of a FK is blocked because the new reference does not exist,
- when 2 changes on a tuple are inconsistent (del/upd, different values (null vs. a value),
- rules that derive the modifications to be finally executed.

Results

- if an update set is admissible, the well-founded model is sufficient: giving priorities to modifications/propagations/changes vs. blockings yields a total stable model and the updates to be executed
- if an update set is not admissible, the stable models indicate what portions of the initial set are admissible, and where the problems are located (mutually excluding updates, missing cascades, unresolved tuples).

12.3 The Limits

Recall:

 ASP is based on atoms (i.e., disjunction is not dealt with as formula, but resolved into atoms)

(note: in tableaux, it is also broken down to atoms)

- ASP algorithms are internally based on ground atoms and grounding of all rules (with all ground terms=constants of the Herbrand universe).
 (note: tableaux can keep variables and use them on-demand)
- ASP is closely related with Model Checking: generate models by a strategy.

Expressiveness

- Datalog[¬] rules, for ASP extended with:
 - disjunction/choice rules: generate suitable different models (cf. tableau: branches)
 - negation: via denials. Discard models.
 (cf. tableau: close branch)

722

The Limits

The Limits of ASP:

- no existential quantification, object invention:
 - every person has a father who is again a person. (tableau: via skolemization and strategical application of the δ -rule)
 - ASP/grounding: would require infinitely many ground instances.
 (tableau: strategic application of the γ-Rule + Blocking strategies (e.g., DL/OWL reasoning))
- *P* ⊨ *a* means only that *a* holds in the minimal/stratified/well-founded model.
 Statements about ¬*a* only by default negation/closed world.
 (On the other hand: LP provides a CWA reasoning formalism in contrast to tableaux)

Comparison: Tableaux

- Tableaux can be tailored to any logic: FOL, DL/OWL, ...
 - Open-World: monotonic
 - complex expansion & blocking strategies + heuristics.
- ASP is worst-case exponential, but with a polynomial basis: the AFP computation for the well-founded model.

12.4 DB vs. KB: Closed World vs. Open World

Consider the following formula *F*:

 $F \equiv person("John", 35) \land person("Alice", 10) \land person("Bob", 8) \land \land person("Carol", 12) \land person("Jack", 65) \land \land child("John", "Alice") \land child("John", "Bob") \land \forall X, Y : (\exists Z : (child(Z, X) \land child(Z, Y) \land X \neq Y) \rightarrow sibling(X, Y))$

- Does *child*("John", "Bob") hold? obviously yes.
- Does *G*:≡*sibling*("Alice", "Bob") hold?
 - (Relational) Database: *sibling* is a view. The answer is "yes".
 - FOL KB: for all models \mathcal{M} of F, G holds. Thus, $F \models sibling($ "Alice", "Bob").
- What about G:=sibling("Alice", "Carol")?
 - (Relational) Database: no. For the database state $\mathbf{D}, \mathbf{D} \not\models sibling$ ("Alice", "Carol").
 - FOL KB: there is a model \mathcal{M}_1 of F, where $\mathcal{M}_1 \not\models G$, but there is also a model \mathcal{M}_2 of F, where $\mathcal{M}_2 \models G$ (e.g., add the tuple ("John", "Carol") to the interpretation of *child*).

For the Web, $\mathit{child}("John", "Carol")$ can e.g. be contributed by another Web Source.

724

DB vs. KB: CLOSED WORLD vs. OPEN WORLD

- What about G := child("John", "Jack")?
 - (Relational) Database: no. For the database state \mathbf{D} , $\mathbf{D} \not\models child$ ("John", "Jack").
 - FOL KB: there is a model \mathcal{M}_1 of F, where $\mathcal{M}_1 \not\models G$, but there is also a model \mathcal{M}_2 of F, where $\mathcal{M}_2 \models G$.
- Obviously, the KB does not know that a child cannot be older than its parents. Add a constraint to *F*, obtaining *F*':

 $F' :\equiv F \land \forall P, C, A_1, A_2, : (person(P, A_1) \land person(C, A_2) \land child(P, C)) \rightarrow A_1 > A_2$

- database: this assertion would prevent to add *child*("John", "Jack") to the database.

– for the KB, $F' \models \neg child$ ("John", "Jack") allows to *infer* that Jack is not the child of John. Such information can be given with the *ontology* of a domain.

DB vs. KB: CLOSED WORLD vs. OPEN WORLD

- the Database Model Theory is called "Closed World": things that are not known to hold are assumed not to hold.
- the FOL semantics is called "Open World": things that are not known to be true or false are considered to be possible.

CONSEQUENCES ON NEGATION

- in databases there is no explicit negation. It is not necessary to specify that Jack is *not* a child of John.
- in a KB, it would be necessary to state ... ∧ ¬*child*("John", *X*) for all persons who are known not to be children of John.
 Additional constraints: extend the ontology, e.g., by stating that a person has exactly two parents then all others cannot be parents works only for persons whose parents are known. Similarly for the "age" constraint from the previous slide.
- note that the semantics of universal quantification (\forall) is also effected: $\forall X : \phi$ is equivalent to $\neg \exists X : \neg \phi$.

726

REASONING IN PRESENCE OF NEGATION

Obtaining new information (e.g., by finding another Web Source) has different effects on Open vs. Closed world:

- Closed world: conclusions drawn before "Carol is not a child of John", or "John has exactly two children" from less information can become invalid. This kind of reasoning is *nonmonotonic*
- Open world: everything which is not known explicitly is taken into account to be possible (by considering all possible models).

This kind of reasoning is *monotonic*:

 $\mathsf{Knowledge}_1 \subseteq \mathsf{Knowledge}_2 \Rightarrow \mathsf{Conclusions}_1 \subseteq \mathsf{Conclusions}_2$

 Open World can be combined with other forms of nonmonotonic reasoning, e.g., Defaults: "usually, birds can fly". Knowing that Tweety is a bird allows to conclude that it flies.
 Obtaining the information that Tweety is a penguin (which can usually not fly) leads to invalidation of this conclusion.

The current Semantic Web research mainstream prefers Open World without default reasoning.

COMPARISON, MOTIVATION ETC.							
Database vs. FOL							
Relational Databases	relational schema		tuples	es SQL queries		closed world	
FOL	signatur (predica +functio	re ites ons)	facts (atoms)	$\mathcal{S} \models \phi$? (yes/no or answer $\psi \models \phi$? variable bindings)		mostly: open world sometimes closed world	
Situations and tasks							
Given		what to do		how?			
facts/database does $p(\ldots)$ hold in the DE SQL query		ld in the DB?	by combining	data			
facts+constraintsadditionally:(SQL assertions ortest if constraintsFOL formulas)satisfied		equivalent to first situation (query for violating tuples)					
facts (DB)does $p()$ hold in DB+rules?		DB+views application of rules					
facts (DB) knowledge b as FOL form	base KB nulas	is a enta	formula ϕ ailed by DB	3+KB?	reasoning, entailment, KB $\models \phi$?		