

alternative modeling:

capital/1 unary fct: maps country \rightarrow city

capital(germany) = berlin $\in \Sigma$
0-ary function symbols $\in \Sigma$

$\hat{=}$ binary relation: $\frac{\text{country} \mid \text{city}}{\text{germany} \mid \text{berlin}}$

Chomsky/2 binary fct: (country, out) \rightarrow decimal

$I(\text{germany}) \hat{=} \text{ternary relation (containing all its values } \rightarrow \mathcal{D})$
 $=_{\text{def}}$

domain $\mathcal{D} = \{ \text{de}, \text{bln}, \dots \}$
 $I(\text{berlin}) = \text{bln}$

Consider capital/2 as a unary function

term: capital(germany) SYNTAX level

$\mathcal{D}^n \rightarrow \mathcal{D}$: $I(\text{capital}) = \{ \text{de} \mapsto \text{bln}, \text{fr} \mapsto \text{paris} \}$
input "capital" input Germany
 $I(\text{germany}) = \text{de} \in \mathcal{D}$

$I(\text{capital(germany)}) = I(\text{capital})(I(\text{germany}))$
 $= \text{bln} \in \mathcal{D}$

as a query: return $\text{berlin} \in \Sigma$
 the constant symbol that "means" bln .

Formula: $\varphi = \text{capital}(\text{germany}) \doteq \text{berlin}$

is φ true or not? $I(\varphi) = \text{true/false?}$

$\doteq \doteq (\text{capital}(\text{germany}), \text{berlin})$ holds?

$\doteq (\text{capital}(\text{germany}), \text{berlin}) \in I(\doteq)$

if ~~not~~ $I(\text{capital}(\text{germany})) = I(\text{berlin})$

if $\text{bln} = \text{bln}$

which is true

Annotations: "equality on the syntax level", "built-in binary predicate", "same element of \mathcal{D} ", "new variable", "object same \mathcal{D} ".

$I(\text{capital}(x))$

free variables:

FOL: for evaluation: provide a variable binding for x

DD: give us the answers: all possible x .